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CAVITATION RESULTS FOR A SECONDARY FLOW GENERATED

TRAILING VORTEX

M. L. Billet

Techanical Memorandum
File No. TM 76-234

24 August 1976

Contract No. N00017-73-C-1418

Copy No.

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PREPARED UNDER THE NAVAL SEA SYSTEMS COMMAND GENERAL HYDROMECHANICS RESEARCH PROGRAM ADMINISTERED BY THE DAVID W. TAYLOR NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER, (Code 1505), BETHESDA, MD 20084



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SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION	READ INSTRUCTIONS BEFORE COMPLETING FORM								
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		6. PERFORMIN	G ORG. REPORT NUMBER						
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Applied Research Laboratory P. 0. Box 30 State College, PA 16801	35	10. PROGRAM I AREA & WO	ELEMENT, PROJECT, TASK RK UNIT NUMBERS						
11. CONTROLLING OFFICE NAME AND ADDRESS Naval Sea Systems Command		12. REPORT DATE							
Washington, DC 20362		24 August 1976							
mashington, bo 2002		13. NUMBER OF PAGES 22							
14. MONITORING AGENCY NAME & ADDRESS(It ditter	ent from Controlling Office)	UNCLAS	CLASS. (of this report)						
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17. DISTRIBUTION STATEMENT (of the abstract entere	ed in Block 20, if different fro	m Report)	200						
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18. SUPPLEMENTARY NOTES			JUSTIFICATION						
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From: M. L. Billet

Subject: Cavitation Results for a Secondary Flow Generated Trailing

Vortex

References: See page 13.

Abstract: Limited cavitation numbers were obtained for a trailing vortex

generated by the interaction of a boundary layer and a rotor when the boundary layer thickness is the same order of magnitude as the rotor radius. The results were

obtained for various boundary layer profiles and velocities

in the 48-inch diameter water tunnel.

Acknowledgments: This paper is based in part upon research conducted under

the General Hydromechanics Research Program of the Naval Ship Systems Command, technically administered by the David Taylor Naval Ship Research and Development Center, and research sponsored by the Naval Sea Systems Command.

Table of Contents

																						Page
Abstract																						1
Acknowledgments																				•		1
List of Figures																						3
List of Tables																			•			3
Nomenclature .								•			•		•									4
Introduction .										•				•			•					5
Background Info	orma	ti	on									•						•			٠	5
Description of	the	E	хр	er	im	en	ts				•									•		9
Discussion of	Resu	1t	s																			10
Summary								•							•							11
References				•									•									13
Tables																						14
Figures																		٠.				15

List of Figures

Figure No.	<u>Title</u>	Page
1	Tip Designs	15
2	Cavitation Data - Effect of Air Content (Basic Flow #4)	16
3	Cavitation Data - Effect of Tip Design (Basic Flows #4, #10)	17
4	Cavitation Data - Effect of Flow Coefficient (Basic Flows #4, #5, #6)	18
5	Cavitation Data - Effect of Appendages (Basic Flows #1, #4)	19
6	Cavitation Data - Effect of Appendages and Screen (Basic Flows #1, #3, #4, #7)	20
7	Cavitation Data - Effect of Screen and Flow Coefficient with Appendages (Basic Flows #4, #6, #7, #8)	21
. 8	Cavitation Data - Effect of Screen and Flow Coefficient Without Appendages (Basic Flows #1, #3, #2, #9)	22
	List of Tables	
Table No.	<u>Title</u>	Page
1	Basic Flow Configurations	14

Nomenclature

C - characteristic pressure coefficient

 $\mathbf{C}_{\mathbf{p}_{\min}}$ – minimum pressure coefficient

 $\mathbf{P}_{\mathbf{G}}$ - pressure typical of the noncondensable gas in a bubble

 $\mathbf{P}_{\mathbf{G}_{\mbox{\scriptsize max}}}$ - maximum gas pressure in a bubble

 P_{min} - minimum pressure

 $\mathbf{P}_{\mathbf{v}}$ - vapor pressure based on liquid temperature

 $\boldsymbol{P}_{_{\boldsymbol{x}\boldsymbol{x}}}$ — static pressure of infinity

 P_{ω_0} - static pressure at infinity for limited cavitation

 $\mathbf{U}_{\mathrm{TIP}}$ - rotor tip velocity

 V_{∞} - velocity at infinity

α - dissolved gas content of the liquid

β - Henry's Law constant

φ - flow coefficient

σ - cavitation number

od - desinent cavitation number

 σ_{ϱ} - limited cavitation number

ρ - mass density of the liquid

INTRODUCTION

Secondary flows generate additional streamwise vorticity when a boundary layer flow is turned by a rotor. The apparent effect of this additional vorticity is evidenced by a cavitating trailing vortex.

The cavitation number of this vortex which exists in the complicated flow downstream of the rotor is a measure of the amount of streamwise vorticity near the wall of the rotor. In most cases, the critical cavitation numbers typical this trailing vortex system are often higher than those associated with any other type of cavitation.

Vortex cavitation is one of the least understood forms of cavitation.

It is felt that this lack of understanding is due to an inadequate knowledge of the flow field and the effects of noncondensable gases. As an example, the structure of the trailing vortex created in the passage of a rotor is influenced very significantly by variations of the incoming boundary layer to the rotor. Also, vortex flows tend to be good collectors of gas bubbles which can cause nonvaporous cavitation. The cavitation numbers associated with limited nonvaporous cavitation are often considerably higher than those for limited vaporous cavitation.

In this investigation, experimentally determined cavitation numbers for the trailing vortex system were obtained for various incoming boundary layer profiles and flow coefficients. Also, the effect of air content on the cavitation number was determined.

BACKGROUND

Cavitation flows are delineated by the cavitation number, σ , defined as

$$\sigma \equiv \frac{P_{\infty} - P_{V}}{1/2\rho V_{\infty}^{2}} \tag{1}$$

where P_{∞} , V_{∞} , P_{V} and ρ are the pressure at infinity, the velocity at infinity, the vapor pressure, and the mass density of the liquid, respectively. The fluid properties correspond to the bulk temperature of the liquid.

The flow regime of particular concern is limited cavitation, i.e. the extent of cavitation is minimized. The problem of limited cavitation has been reviewed in recent years by Holl [1]* and Holl, Arndt, and Billet [2].

The particular value of σ corresponding to limited cavitation is the limited cavitation number $\sigma_{\ell},$ or critical cavitation number given by

$$\sigma_{\ell} = \frac{P_{\infty} - P_{v}}{(1/2)\rho v_{\infty}^{2}} . \qquad (2)$$

In this investigation, σ_{ℓ} is determined by a desinence test so that

$$\sigma_{\ell} = \sigma_{d}$$
 (3)

where σ_d is the desinent cavitation number [3]. The limited cavitation number can also be determined by an inception test, provided hysteresis effects are not involved [4].

There are two general types of limited cavitation, namely vaporous and nonvaporous cavitation. To visualize the various types of limited cavitation, it is useful to imagine that one is observing the growth of a single bubble as the pressure is suddenly reduced. Vaporour cavitation

 $^{^{\}star}$ Numbers in brackets refer to documents given in the list of references.

the explosive growth of a bubble due to the rapid conversion of liquid to vapor at the bubble wall. There are two types of nonvaporous cavitation, namely pseudo and gaseous cavitation. Pseudo cavitation occurs when a bubble merely expands due to a reduction in pressure with the mass of gas in the bubble essentially remaining constant.

Gaseous cavitation occurs when a bubble grows in an oversaturated liquid due to the transport of gas across the interface. In contrast to vaporous cavitation, nonvaporous cavitation can occur at pressures greater than vapor pressure.

Of particular importance in the study of limited cavitation is the minimum pressure coefficient, $\mathbf{C}_{\mathbf{p}_{\min}},$ given by

$$c_{p_{\min}} = \frac{P_{\infty} - P_{\min}}{1/2\rho \ V_{\infty}^2}$$
 (4)

where \mathbf{p}_{\min} is the minimum pressure.

In general, results indicate for vaporous limited cavitation that

$$\sigma_{\ell} \leq C_{p_{\min}}$$
 (5)

In principle, nonvaporous cavitation can occur below or above vapor pressure [1]. However, from a practical point of view, it is the latter type which is the most interesting because of the large values of cavitation numbers which are often typical of these cases [1]. Thus, for nonvaporous limited cavitation occurring at pressures above vapor pressure

$$\sigma_{\ell} > c_{p_{\min}}$$
 (6)

In 1960, Holl [3] employing an equilibrium theory which ignored surface tension effects predicted for nonvaporous cavitation that

$$\sigma_{\ell} = c_{p} + \frac{P_{G}}{1/2\rho \ V_{\infty}^{2}} \qquad , \tag{7}$$

where $\mathbf{C}_{\mathbf{p}}$ is a characteristic pressure coefficient, and $\mathbf{P}_{\mathbf{G}}$ is a pressure typical of the noncondensable gas in the bubbles. Holl indicated that there was an upper limit to the gas pressure, namely the equilibrium value given by Henry's Law which may be expressed in the form

$$P_{G_{max}} = \alpha \beta$$
 (8)

where α is the dissolved gas content and β the Henry's Law constant.

Several general implications come from Equation (7). Firstly, the equation predicts that σ_{ℓ} is a monotonically decreasing function of velocity for constant values of P_G and C_p . Secondly, the equation predicts excessively large values of σ_{ℓ} at low velocities. These results suggest that, if one is to avoid confusing nonvaporous for vaporous cavitation, it is advisable to conduct tests at high velocities. The aforementioned tendency for σ_{ℓ} to decrease with velocity for nonvaporous cavitation is characteristic of data reported by several authors, namely, Hammitt et al. [5], Lindgren and Johnson [6], McCormick [7], and Ripken and Killen [8].

Thus, it is very important to understand the differences between vaporous and nonvaporous cavitation in order to interpret test data. It

is also apparent in view of Equations (5) and (6) that it is very important to know \mathbf{C}_p in order to differentiate between various flow states. However, in many flows \mathbf{C}_p data are not available so that other means for differentiating between flow states, such as noise spectra, are needed.

DESCRIPTION OF THE EXPERIMENTS

The experiments were conducted with water near room temperature in the 48-inch diameter tunnel located in the Carfield Thomas Water Tunnel Building of the Applied Research Laboratory at The Pennsylvania State University. In all cases, desinent cavitation was employed as the experimental measure of limited cavitation. Limited cavitation in the trailing vortex system occurred at the cone tip which was behind the rotor located at the end of the axisymmetric forebody. Also, the occurrence of the cavitation was very sporadic.

The air content was approximately 3.1 ppm for all of the experiments except for one experiment which had a range of air contents. The air content of 3.1 ppm was chosen because gas effects are reduced and the relative saturation level was always much less than unity.

Desinent cavitation number data were obtained for different incoming velocity profiles to the rotor. The incoming velocity profile was varied by changes in the configuration of the axisymmetric forebody. Results were obtained with/without upstream appendages, with/without a screen on the nose of the axisymmetric forebody, and on/off design rotor flow coefficients. In addition, two different tip designs were employed behind the rotor. These basic flows are described in Table 1 and the tip designs are sketched in Figure 1.

DISCUSSION OF RESULTS

The desinent cavitation number data are shown in Figures 2-8 where the effects of the following factors are displayed:

Figure 2 - Effect of Air Content

Figure 3 - Effect of Tip Design

Figure 4 - Effect of Flow Coefficient

Figure 5 - Effect of Upstream Appendages

Figure 6 - Effect of Upstream Appendages and Screens

Figure 7 - Effect of Screen and Flow Coefficient with Appendages

Figure 8 - Effect of Screens and Flow Coefficient without Appendages

Thus, Figures 2-8 display the effects of air content, tip design, flow coefficient, upstream appendages, and upstream screens on the desinent cavitation number.

In general, an increase in gas content, the addition of upstream appendages, or a 10% decrease in flow coefficient cause the cavitation number to increase. In contrast to these results, the addition of upstream screens or a 10% increase in flow coefficient cause the cavitation number to decrease.

Data in Figure 4 shows that a decrease in the flow coefficient by 10% causes a dramatic increase in the cavitation number, whereas a 10% increase in the flow coefficient causes the opposite trend. The cavitation number at the design flow coefficient increases slowly with velocity, whereas at 10% below the design flow coefficient, it increases rapidly with velocity. In contrast to these trends, at a flow coefficient 10% above the design value, the cavitation number decreases with velocity.

The effect of upstream appendages is displayed by the data in Figures 5 and 6, where the appendages are in the form of four struts upstream of the rotor. It is seen that the addition of the appendages increases the cavitation number by 50 to 70%.

The effect of tip design is shown by the data in Figure 3. The data indicates that the conical tip causes cavitation numbers which increase with velocity and range between 4.5 and 5.1. In contrast to this trend, the truncated conical tip causes much higher cavitation numbers which tent to decrease with an increase in velocity. This velocity trend is in agreement with the equilibrium theory discussed in the background information. Assuming that C_{pmin} and P_{G} are essentially constant, then Equation (7) can be expressed as

$$\sigma_{\rm d} = {\rm constant} + \frac{{\rm constant}}{{\rm V_{\infty}}^2}$$
 (9)

The data for the truncated cone tip approximate this trend. Apparently, the separated flow increases the residence time of bubbles in the low pressure region which accentuates the gas effects predicted by the equilibrium theory.

The data in Figure 2 also show gas effects on the cavitation number.

As the gas content increases, the cavitation number tends to increases.

SUMMARY

Cavitation numbers for trailing vortex cavitation from a rotor vary significantly with upstream configurations. Variations in the shape of the incoming boundary layer influences the loading on the rotor near the hub. This causes variations in the amount of inlet vorticity to the rotor passage and variations in the amount of secondary vorticity generated in the blade passage. Small changes in the profile result in

a large increase in the cavitation number as shown by the addition of upstream appendages. A 10% decrease in the flow coefficient causes an increase in σ whereas a 10% increase in the flow coefficient yields the opposite trend. The cavitation number is sensitive to air content effects, particularly for the truncated conical tip design.

REFERENCES

- 1. J. W. Holl, "Limited Cavitation," Proceedings of the Symposium on Cavitation State of Knowledge, ASME, June 1969, pp. 26-63.
- J. W. Holl, R. E. A. Arndt, and M. L. Billet, "Limited Cavitation and the Related Scale Effects Problem," Proc. Second Int. JSME Symp. on Fluid Machinery and Fluidics, Tokyo, September 1972, pp. 303-314.
- J. W. Holl, "An Effect of Air Content on the Occurrence of Cavitation," <u>Journal of Basic Engineering</u>, Trans. ASME, Series D, Vol. 82, 1960, <u>pp. 941-946</u>.
- J. W. Holl and A. L. Treaster, "Cavitation Hysteresis," <u>Journal of Basic Engineering</u>, Trans. ASME, Series D, March 1966, pp. 199-212.
- 5. F. G. Hammitt, J. F. Lafferty, D. M. Ericson, and M. J. Robinson, "Gas Content, Size, Temperature and Velocity Effects on Cavitation Inception in a Venturi," ASME Paper 67 WA/FE 22, 1967.
- 6. H. Lindgren and C. A. Johnson, "Cavitation Inception on Head Forms ITTC Comparative Experiments," Report No. 58, Swedish State Shipbuilding Experimental Tank, 1966.
- B. W. McCormick, "On Cavitation Produced by a Vortex Trailing from a Lifting Surface," <u>Journal of Basic Engineering</u>, Trans. ASME, September 1962, pp. 369-379.
- 8. J. F. Ripken and J. M. Killen, "Gas Bubbles: Their Occurrence, Measurements, and Influence in Cavitation Testing," Proceedings of IAHR Symposium, Sendai, Japan, 1962, pp. 37-57.

TABLE 1

Basic Flow Configurations

Tip Design	Conical	Conical	Conical	Conical	Conical	Conical	Conical	Conical	Conical	Truncated - Conical
Rotor Flow Coefficient (ϕ)	$*^{P}\phi = \phi$	$P_{\phi 6.0} = \phi$	P _Φ = Φ	Рф. #	$\phi = 1.1\phi_{d}$	$p_{\phi 6.0} = \phi$	Р ф = ф	$^{P}\phi$ 6.0 = ϕ	$P = 0.9\Phi$	$P_{\phi} = \phi$
Upstream	No	No	Yes	No	No	No	Yes	Yes	Yes	No
Upstream Appendages**	No	No	No	Yes	Yes	Yes	Yes	Yes	No	Yes
Number	н	7	8	7	5	9	7	8	6	10

 * φ_d = design flow coefficient ${\rm \fomalign{2} V_{\infty}/U_{TIP}}$

** The upstream appendages consisted of four struts placed at the 0°, 90°, 180°, 270° points on the axisymmetric test body.



TRUNCATED CONICAL TIP



CONICAL TIP

Figure 1 - Tip Designs

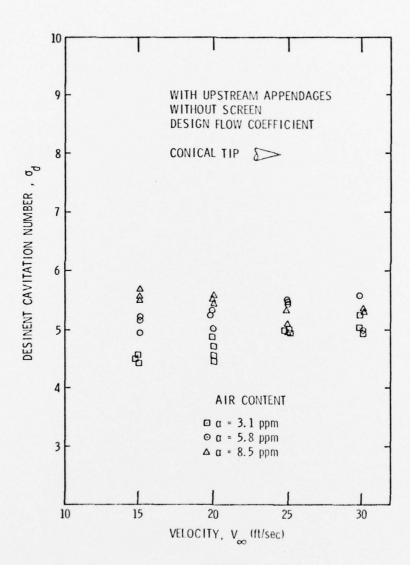


Figure 2 - Cavitation Data - Effect of Air Content (Basic Flow #4)

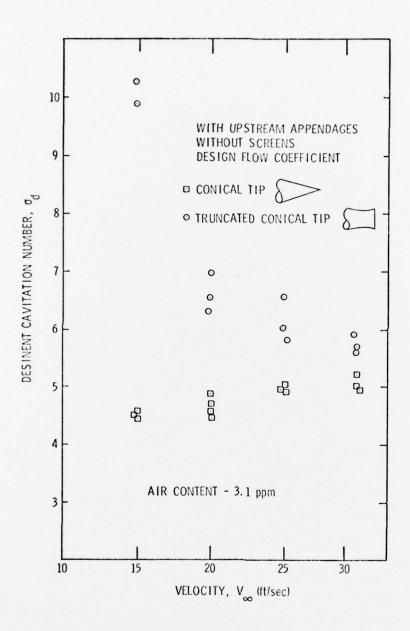


Figure 3 - Cavitation Data - Effect of Tip Design (Basic Flows #4, #10)

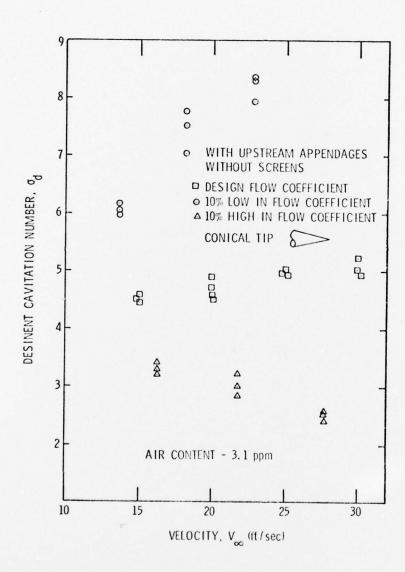


Figure 4 - Cavitation Data - Effect of Flow Coefficient (Basic Flows #4, #5, #6)

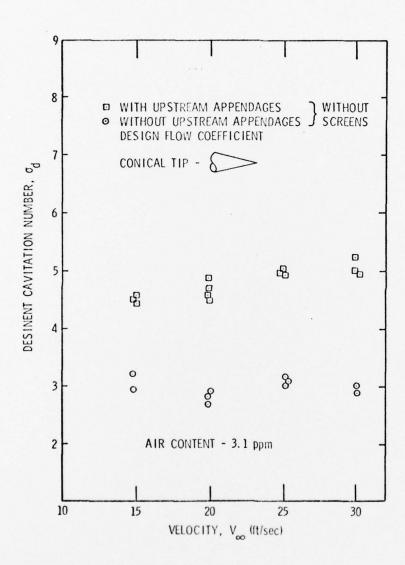


Figure 5 - Cavitation Data- Effect of Appendages (Basic Flows #1, #4)

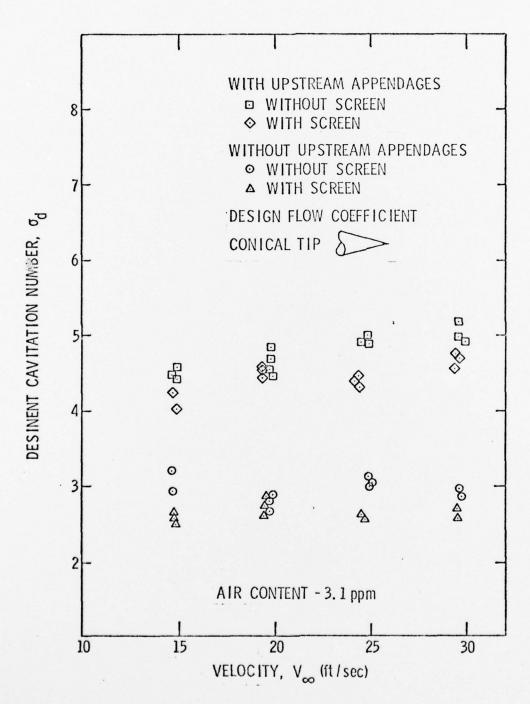


Figure 6 - Cavitation Data - Effect of Appendages and Screen (Basic Flows #1, #3, #4, #7)

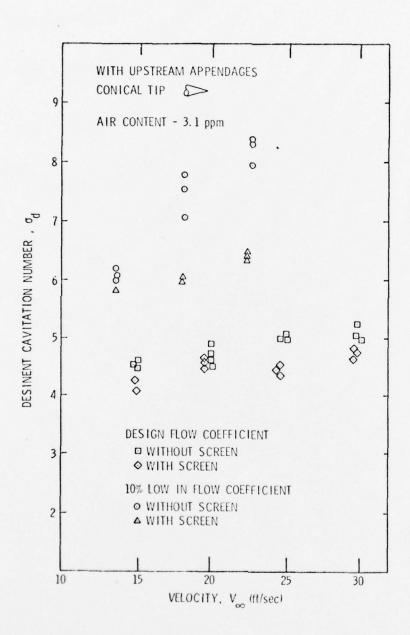


Figure 7 - Cavitation Data - Effect of Screen and Flow Coefficient with Appendages (Basic Flows #4, #6, #7, #8)

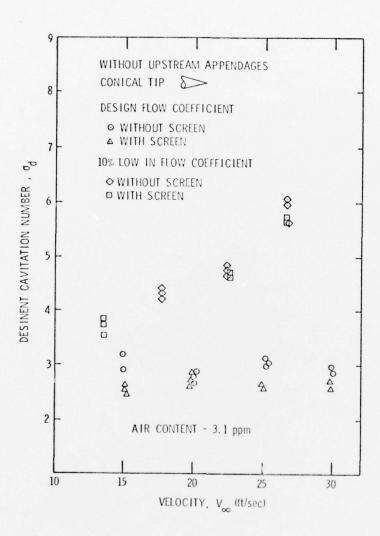


Figure 8 - Cavitation Data - Effect of Screen and Flow Coefficient Without Appendages (Basic Flows #1, #2, #9)